

warm-UP : Factor!

$$\textcircled{1} (b-1) \left( \frac{(b-1)a^2 + 2(b-1)a - 8(b-1)}{b-1} \right)$$

$$(b-1)(a^2 + 2a - 8)$$

$$\begin{array}{r|l} \otimes -8 & (1, -8), (-1, 8), (2, -4), (-2, 4) \\ \oplus +2 & -7 \quad 7 \quad -2 \quad 2 \end{array}$$

$$(b-1)(a-2)(a+4) \quad \text{Check}$$

Today, we will be factoring  
 $ax^2 + bx + c$

$$\begin{array}{r|l} \otimes a \cdot c & \\ \oplus b & \end{array}$$

$$\textcircled{2} (x^2 - 8x + 16) - y^2$$

*Perfect Square Quadratic*

$$\begin{array}{r|l} \otimes 16 & (1, 16), (4, 4), (-4, -4), (2, 8), (-2, -8), (-1, -16) \\ \oplus -8 & 17 \quad 8 \quad -8 \end{array}$$

$$(x-4)(x-4) - y^2$$
$$(x-4)^2 - y^2$$

$$\sqrt{1^{\text{st}}} = \sqrt{(x-4)^2} = (x-4) \quad \leftarrow 'a'$$

$$\sqrt{2^{\text{nd}}} = \sqrt{y^2} = y \quad \leftarrow 'b'$$

$$\underline{(x-4-y)(x-4+y)}$$

Find  $p, q$  so that

$$p \cdot q = a \cdot c \quad \underline{\text{and}} \quad p + q = b$$

$p, q$  are not factors anymore

Ex 1 Factor  $6x^2 + 11x + 4$

$$6 \cdot 4 = a \cdot c$$

$\otimes +24$	$(1, 24)$	$(2, 12)$	$(3, 8)$	$(4, 6)$
$\oplus +11$	25	14	11	10

② Split our middle term

$$6x^2 + 3x + 8x + 4$$

③ Factor each pair

$$(6x^2 + 3x) + (8x + 4)$$

$$3x(2x + 1) + 4(2x + 1)$$

④ Factor out Common factor from the pairs

$$(2x+1)(3x+4) \quad \text{check}$$

$$= 6x^2 + 8x + 3x + 4 = 6x^2 + 11x + 4$$

(11)

Ex 2 Factor

$$-4x^2 - 14x + 8$$

$$= -2(2x^2 + 7x - 4)$$

$2x-4$

$\otimes -8$	$(-1, 8)$	$(-2, 4)$	$(2, -4)$	$(1, -8)$
$\oplus 7$	$7$			

$$\begin{aligned}
 &= -2(2x^2 - x + 8x - 4) \\
 &= -2(x(2x - 1) + 2(4x - 2)) \\
 &= -2(x(2x - 1) + 4(2x - 1)) \\
 &= -2[(2x - 1)(x + 4)] \\
 &= -2((2x^2 + 8x) + (-x - 4)) \\
 &= -2[2x(x + 4) - 1(x + 4)] \\
 &= -2[(x + 4)(2x - 1)]
 \end{aligned}$$

## Special Case #2

Perfect Square quadratics

Notice  $(a + b)^2 = (a + b)(a + b) = a^2 + ab + ab + b^2$

$(a + b)^2 = a^2 + 2ab + b^2$

$$(a-b)^2 = (a-b)(a-b) = a^2 - ab - ab + b^2$$
$$(a-b)^2 = a^2 - 2ab + b^2$$

If the first and last term are positive and perfect squares, check middle term

If middle term =  $\pm 2 \sqrt{\text{1st}} \cdot \sqrt{\text{last}}$   
We have a perfect square.

Ex 3                      Factor

$$4x^2 + 12x + 9$$

$$\sqrt{\text{1st}} = \sqrt{4x^2} = 2x \quad \leftarrow a$$

$$\sqrt{\text{last}} = \sqrt{9} = 3 \quad \leftarrow b$$

check middle:  $\pm 2(2x)(3) = \textcircled{+} 12x$

$$= (2x + 3)^2$$

Ex 4 Factor  $-2a^3 + 8a^2b - 8ab^2$

$$= -2a(a^2 \textcircled{-} 4ab + 4b^2)$$

$$\sqrt{\text{1st}} = \sqrt{a^2} = a$$

$$\sqrt{\text{last}} = \sqrt{4b^2} = 2b$$

check  $\pm 2(a)(2b) = \pm 4ab$   
 $= -2a(a - 2b)^2$

## Summary

1. Common factors!
2. Special cases (Diff. Sq.  $\text{\textcircled{or}}$  Perf. Sq.)  
(1st and last term are perf. Sq. then probably a Special case)

3.  $x^2 + bx + c \Rightarrow$  use what we learned yesterday

4.  $ax^2 + bx + c \Rightarrow$  use what we learned today

5. Check!

Mon: work time

wed: Quiz