

Warmup (Quiz Friday on 2.2-2.4)

① What is the maximum product of two numbers that add to give 22. What are the numbers?

② Equations & Variables ← what ever you want to max or min  
stuff you don't know

$$\underline{a+b} \Rightarrow \underline{at+b=22}$$

max  
 $\Rightarrow$  vertex

$$\text{Product} = \underline{a \cdot b = P}$$

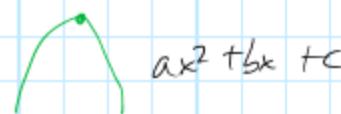
$$P = a \cdot b$$

$$a+b = 22$$

$$P = a(22-a)$$

$$b = 22-a$$

$$\underline{P} = 22a - a^2$$



$$\underline{\text{Vertex}}: h = \frac{-b}{2a} = \frac{-(22)}{2(-1)} = \frac{-22}{-2} = 11$$

$x$  value of vertex  $\Rightarrow$  a value for max

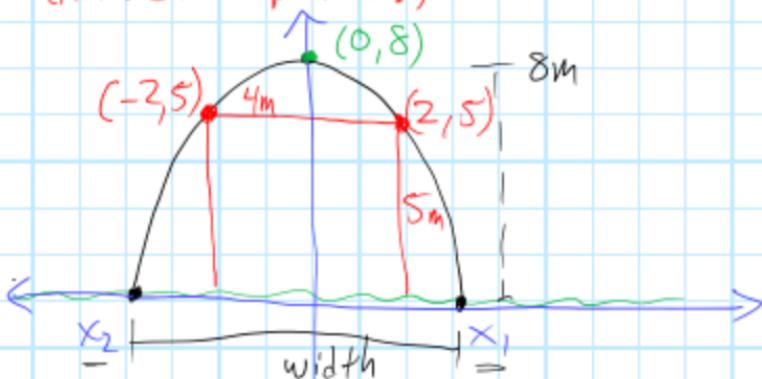
$$\underline{a, b} \quad \underline{a=11} \Rightarrow b = 22-a \\ = 22-11$$

2 #'s are 11 and 11

$$\text{max product} = 11 \cdot 11 = \boxed{121}$$

② A parabolic arch is 8 m tall. If a rectangular truck that is 5 m tall and 4 m wide must fit through the arch, how wide must the arch be at the bottom? (Answer exactly and to 1 decimal place)

(Hint: draw a picture!)



(equation of arch)

$$y = a(x - h)^2 + k$$

$$h=0 \quad k=8$$

$$y = ax^2 + 8 \quad \text{Point } (2, 5)$$

$$f(2) = 5 = a(2)^2 + 8$$

$$5 = 4a + 8 \Rightarrow -3 = 4a$$

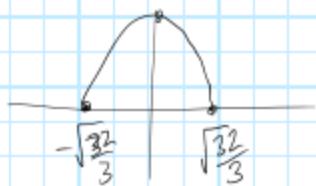
$$a = -\frac{3}{4}$$

$$f(x) = -\frac{3}{4}x^2 + 8 = 0 \quad (\text{x-intercepts})$$

$$-\frac{4}{3} \cdot -\frac{3}{4}x^2 = -8 \cdot -\frac{4}{3}$$

$$x^2 = \frac{32}{3}$$

$$x = \pm \sqrt{\frac{32}{3}} = \pm 3.3$$



$$\begin{aligned}\text{Width} &= 2\left(\sqrt{\frac{32}{3}}\right) = \boxed{2\sqrt{\frac{32}{3}}} \\ &= 2(3.3) = \boxed{6.6}\end{aligned}$$

Quiz 2.2 - 2.4 Friday  
Completing the square  
on it

Schedule

Tu NOV 5 - Collab % Give back Quiz

th NOV 7 - Assemblies / Review  
Math Contest

wed NOV 13 - Test chp 2 (Block flip)