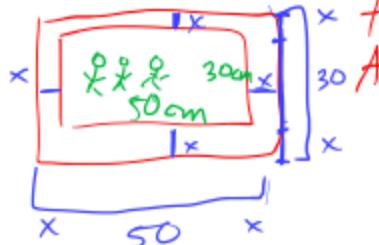


Ex 1 A 30cm by 50cm picture has a frame surrounding it. If the frame is the same width all around, and the total area of the frame and picture is 1836 cm^2 , how wide is the frame?



check $x=2$

$$1836 = (50+4)(30+4)$$

$$1836 = 1836 \checkmark$$

$$\begin{aligned} \text{total Area} &= 1836 = (50+2x)(30+2x) \\ -1836 &\quad -1836 \\ 1836 &= 1500 + 60x + 100x + 4x^2 \end{aligned}$$

$$0 = 4x^2 + 160x - 336$$

$$0 = 4[(x^2 + 40x + 400) - 400] - 336$$

$$0 = 4[(x+20)^2 - 400] - 336$$

$$0 = 4(x+20)^2 - 400 \cdot 4 - 336 \Rightarrow 4(x+20)^2 - 1936 = 0$$

Ex 2 The sum of a number and three times its reciprocal is $\frac{28}{3}$. What is the number?

x - the number

$$x\left(x + 3 \cdot \frac{1}{x}\right) = \left(\frac{28}{3}\right)x$$

$$3(x^2 + 3) = \left(\frac{28}{3}x\right) \cdot 3$$

$$3x^2 + 9 = 28x$$

$$3x^2 - 28x + 9 = 0$$

$$3x^2 - x - 27x + 9 = 0$$

$$x(3x-1) - 9(3x-1) = 0$$

$$(3x-1)(x-9) = 0$$

$$\begin{array}{l} 3x-1=0 \\ x=\frac{1}{3} \end{array} \quad \begin{array}{l} x-9=0 \\ x=9 \end{array}$$

$$\textcircled{Q} 27 \mid (-1, -27)$$

$$\textcircled{P} -28 \mid -28$$

check $x=9$

$$9 + 3 \frac{1}{9}$$

$$= 9 + \frac{1}{3} = \frac{27}{3} + \frac{1}{3} = \frac{28}{3} \checkmark$$

check $x=\frac{1}{3}$

$$\frac{1}{3} + 3 \cdot \frac{1}{\left(\frac{1}{3}\right)}$$

$$= \frac{1}{3} + 9 = \frac{28}{3} \checkmark$$

$$1 \div \frac{1}{3} = 1 \cdot \frac{3}{1} = 3$$

$$(x+20)^2 = 1936$$

$$(x+20)^2 = 484$$

$$x+20 = \pm 22$$

$$x = -20 \pm 22$$

$$x = 2 \quad \text{neg width}$$

school. If they both leave at the same time, Mrs. Anderson gets to school 12 minutes before Mr. Raoul. If Mrs. Anderson drives 15km/h faster than Mr. Raoul can bike, what is the speed of each of them (answer to 1 decimal place)?

	DST	Speed	time	$D = s \cdot t$
Mr. R	8 km	y	t	
Mrs. A	8 km	$y + 15 \frac{\text{km}}{\text{h}}$	$t - 0.2 \text{ min}$ $t - 0.2 \text{ h}$	$\frac{12}{60} = \frac{1}{5} = 0.2$

$$8 = y \cdot \frac{8}{y} + y \cdot (-0.2) + 15 \cdot \frac{8}{y} + 15 \cdot (-0.2)$$

$$8 = y \cdot t \quad \leftarrow t = \frac{8}{y}$$

$$8 = (y + 15)(t - 0.2)$$

$$8 = (y + 15)\left(\frac{8}{y} - 0.2\right)$$

$$8 = 8 - 0.2y + \frac{120}{y} - 3$$

$$y \cdot 0 = (-0.2y + \frac{120}{y} - 3)y$$

$$0 = -0.2y^2 + 120 - 3y$$

$$\begin{array}{l} a = -0.2 \\ b = -3 \\ c = 120 \end{array}$$

$$y = \frac{-(-3) \pm \sqrt{(-3)^2 - 4(-0.2)(120)}}{2(-0.2)} = \frac{(3 \pm \sqrt{9 + 96})}{-0.4}$$

$$\text{Mr. R} \Rightarrow 18.1 \frac{\text{km}}{\text{h}}$$

$$\begin{aligned} \text{Mrs. A} &\Rightarrow 18.1 \frac{\text{km}}{\text{h}} + 15 \frac{\text{km}}{\text{h}} \\ &= 33.1 \frac{\text{km}}{\text{h}} \end{aligned}$$

Mr. R
Y = Speed

$$= 18.1, -33.1$$

Ex 4 Mr. G and Mrs. Holman are marking PC 11 exams. Mrs. Holman can mark a class set of exams 10 minutes faster than Mr. G can. If they both work together, they can mark a class set in 1 hour. How long does it take each of them to mark a class set of exams (answer to the nearest minute)?

	time to mark 1 class	Rate = $\frac{\text{Amount}}{\text{Time}}$
Mr. G	$x \text{ min}$	$\frac{1 \text{ class}}{x \text{ min}} = \frac{1}{x}$
Mrs. H	$x - 10 \text{ min}$	$\frac{1 \text{ class}}{x - 10 \text{ min}} = \frac{1}{x - 10}$

$$(x-10) \left(\frac{1}{x} + \frac{1}{x-10} \right) = \frac{1}{60} (x-10)$$

Combined: $\frac{1}{x} + \frac{1}{x-10} = \frac{1 \text{ class}}{1 \text{ h}} = \frac{1 \text{ class}}{60 \text{ min}}$

$$\begin{array}{r} 1 \text{ test/min} \\ + 2 \text{ test/min} \\ \hline 3 \text{ test/min} \end{array}$$

$$(x-10) \left(\frac{1}{x} + \frac{1}{x-10} \right) = \frac{1}{60} (x-10) \quad \text{Combined: } \frac{1}{x} + \frac{1}{x-10} = \frac{1}{1 \text{ h}} = \frac{1 \text{ class}}{60 \text{ min}}$$

$$x \left(\frac{x-10}{x} + 1 \right) = \left(\frac{1}{60} (x-10) \right) x$$

$$60(x-10+x) = \left(\frac{1}{60} \times (x-10) \right) 60$$

$$60x - 600 + 60x = x^2 - 10x$$

$$0 = x^2 - 10x - 60x - 600$$

$$0 = x^2 - 130x + 600$$

$$a = 1$$

$$b = -130$$

$$c = 600$$

$$x = \frac{-(-130) \pm \sqrt{(-130)^2 - 4(1)(600)}}{2(1)}$$

$$x = \frac{130 \pm \sqrt{16900 - 2400}}{2}$$

$$x = \frac{125.2}{\cancel{4.8}} \text{ min}$$

↑
Mr. G
marking
time

$$\text{Mr. G} \Rightarrow \boxed{125 \text{ min}}$$

$$\text{Mrs. H} \Rightarrow 125 - 10 \boxed{115 \text{ min}}$$