

① Solve by factoring: $\sqrt{7-4x} = 2-2x$

$$7-4x = (2-2x)^2$$

$$7-4x = 4-8x+4x^2$$

$$0 = 4x^2 - 4x - 3$$

$$= (2x-3)(2x+1)$$

$$x = \frac{3}{2}, \frac{-1}{2}$$

$$\sqrt{7-4x} = 2-2x$$

$$\sqrt{9} = 2+1$$

$$3 = 3$$

Check: $\sqrt{7-4x} = 2-2x$
 $\sqrt{7-4 \cdot \frac{3}{2}} = 2-2 \cdot \frac{3}{2}$

$$\sqrt{7-6} = 2-3$$

$$1 = -1$$

$$a^2 - b^2 = (a+b)(a-b)$$

② Solve by Completing the Square: $\left(\frac{-2}{x-2} + \frac{3x}{x+2} = \frac{-8}{x^2-4}\right) (x-2)(x+2) \Rightarrow (x-2)(x+2)$

$$-2(x+2) + 3x(x-2) = -8$$

$$-2x - 4 + 3x^2 - 6x = -8$$

$$3x^2 - 8x + 4 = 0$$

$$3\left(x^2 - \frac{8}{3}x\right) + 4$$

$$\frac{8}{3} \div 2 = \left(\frac{4}{3}\right)^2 = \frac{16}{9}$$

$$3\left(x^2 - \frac{8}{3}x + \frac{16}{9}\right) + 4 - \frac{16}{9} \times 3 = 0$$

$$3\left(x - \frac{4}{3}\right)^2 + 4 - \frac{16}{3} = 0$$

$$3\left(x - \frac{4}{3}\right)^2 = \frac{4}{3}$$

$$\left(x - \frac{4}{3}\right)^2 = \frac{4}{9}$$

$$x - \frac{4}{3} = \pm \sqrt{\frac{4}{9}}$$

$$x = \pm \frac{2}{3} + \frac{4}{3}$$

$$x = \frac{6}{3}, \frac{2}{3}$$

③ Solve using the quadratic formula: $\frac{1}{2}x^4 - 6x^2 + 10 = 0$
Let $z = x^2$

③ Solve using the quadratic formula : $\frac{1}{2}x^4 - 6x^2 + 10 = 0$

$$X = \pm \sqrt{10}, \pm \sqrt{2}$$

$$\text{Let } Z = X^2$$

$$\frac{-(-6) \pm \sqrt{(-6)^2 - 4 \cdot \frac{1}{2} \cdot 10}}{2 \times \frac{1}{2}}$$

$$2 \times \frac{1}{2}$$

$$Z = X^2$$

$$X^2 = 10, 2$$

$$Z = 10, 2$$

$$X = \pm\sqrt{10}, \pm\sqrt{2}$$

we have 4 answers

④ Jerry and Millie are washing cars. Working alone, Jerry takes 5 minutes more than Millie to wash a car. Working together, it takes them 10 minutes.

a) How long does it take Millie to wash a car?

b) How long does it take Jerry to wash a car?

	time	Rate
Jerry	$x+5$ min	$\frac{1}{x+5}$
Millie	x	$\frac{1}{x}$
together	10 min	$\frac{1}{10}$

Add the rates
 $\Rightarrow \frac{1}{x+5} + \frac{1}{x} = \frac{1}{10}$

$$x(x+5) \left(\frac{1}{x+5} + \frac{1}{x} \right) = \left(\frac{1}{10} \right) x(x+5)$$

$$x(x+5) \cdot \frac{1}{x+5} + x(x+5) \cdot \frac{1}{x} = 0.1 \cdot (x^2 + 5x)$$

$$x + x+5 = 0.1x^2 + 0.5x$$

$$0 = 0.1x^2 - 1.5x - 5$$

$$x = \frac{-(-1.5) \pm \sqrt{(-1.5)^2 - 4(0.1)(-5)}}{2(0.1)}$$

$$= \frac{1.5 \pm \sqrt{2.25 + 2}}{0.2} = 17.81, -2.81$$

neg time

a) 17.81 min

b) 22.81 min