

WARM - UP

$$\textcircled{1} \quad -\sqrt{6^2} + \sqrt{12^2} = -6 + 12 \\ = \boxed{6}$$

$$\textcircled{2} \quad \sqrt{-6^2 + 10^2} = \sqrt{-36 + 100}$$

$$(-6)^2 = -6 \times -6 = 36$$

$$\textcircled{-6}^2 = \textcolor{blue}{-} 6 \times \textcolor{blue}{6} = \textcolor{red}{36}$$

$$= \sqrt{64}$$

$$= \boxed{8}$$

$$\textcircled{3} \quad (\sqrt{9} + \sqrt{4})^2 = (3+2)^2$$

$$\Rightarrow (\sqrt{9})^2 + (\sqrt{4})^2 = (5)^2$$

$$= 9 + 4 = \boxed{25}$$

$$7b) C = 600 \sqrt{A}$$

$$i) \frac{1200}{600} = \frac{600\sqrt{A}}{600}$$

$$(2)^2 = (\sqrt{A})^2$$

$$2^2 = \boxed{A = 4}$$

$$\text{ii) } \frac{2400}{600} = \frac{600\sqrt{A}}{600} \Rightarrow (4)^e = (\sqrt{A})^2$$

$16 = A$

Math 9 Section 1.3 – Pythagorean Theorem

Homework: Section 1.3; 1-3 all, 6-7 even, 8-11 – Answers on Pg. 362

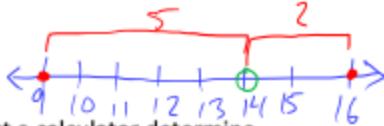
(Don't use a calculator for questions in #2 and #3)

From last classes, we know we can calculate square roots with our calculator, but how do we estimate square roots if the number isn't a perfect square?

Example: Estimate $\sqrt{14}$ without a calculator!

$$\sqrt{9} < \sqrt{14} < \sqrt{16}$$

$$3 < \sqrt{14} < 4$$



Estimate: Closer to 4

Guess: 3.7, 3.8

$$\text{check: } (3.7)^2 = 13.69$$

$$(3.8)^2 = 14.44$$

Between 3.7 and 3.8

For each example below, without a calculator determine...

1) between which two integers is the value of the square root?

2) which one is it closer to? 100, 121, 144, 169

$$\sqrt{39}$$

$$6 < \sqrt{39} < 7$$

$$\sqrt{162}$$

$$12 < \sqrt{162} < 13$$

$$-\sqrt{105}$$

$$-10 > -\sqrt{105} > -11$$

$$6 < \sqrt{39} < 7$$

$$39 \text{ is closer to } 36$$

$$\text{so } \sqrt{39} \text{ is closer to } 6$$

$$12 < \sqrt{162} < 13$$

$$\text{Closer to } 13$$

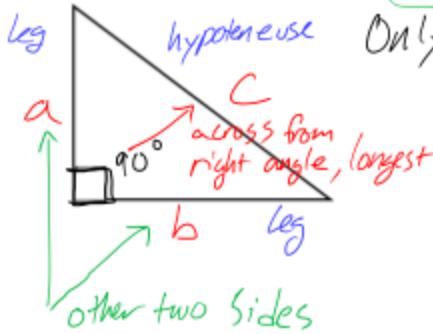
$$\text{since } 162 \text{ is closer to } 144$$

$$-10 > -\sqrt{105} > -11$$

$$\text{Closer to } -10$$

$$\text{because } 105 \text{ is closer to } 100$$

Pythagorean Theorem:



Only works for 90° right triangles

$$\textcircled{1} \quad a^2 + b^2 = c^2 \quad (\text{Solve for } c)$$

$$\textcircled{2} \quad a^2 = c^2 - b^2 \quad (\text{Solve for } a)$$

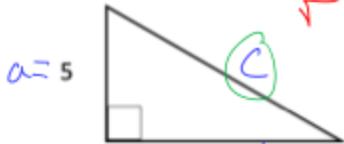
$$\textcircled{3} \quad b^2 = c^2 - a^2 \quad (\text{Solve for } b)$$

How to solve for missing side of a right triangle

- 1) Label each side of the triangle with the letters a, b, c
- 2) Figure out which equation to use
- 3) Put in numbers and simplify the right-hand side
- 4) Don't forget to Square root at the end!

Be Careful!

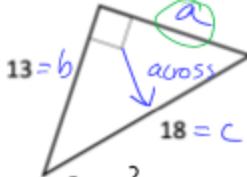
Solve for the missing side exactly, then to one decimal place (if needed):



$$\begin{aligned} C^2 &= a^2 + b^2 \\ C^2 &= 5^2 + 12^2 \\ C^2 &= 25 + 144 \\ C^2 &= 169 \end{aligned}$$

$$C^2 = \sqrt{169}$$

$$C = 13$$



$$\begin{aligned} a^2 &= c^2 - b^2 \\ a^2 &= 18^2 - 13^2 \\ a &= \sqrt{324 - 169} \\ a &= \sqrt{155} \end{aligned}$$

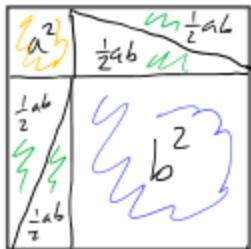
$$a = 12.4$$

1 decimal place

exact

Proof for Pythagorean Theorem: Try to find 2 ways to cover the white square

#1)



#3) Label the sides of the green triangle



$$\begin{aligned} \text{Area} &= \frac{1}{2} \text{base} \times \text{height} \\ &= \frac{1}{2} ab \end{aligned}$$

$$\begin{aligned} a^2 + b^2 + 4\left(\frac{1}{2}ab\right) &= c^2 + 4\left(\frac{1}{2}ab\right) \\ a^2 + b^2 &= c^2 \end{aligned}$$

(11)