

Defining 0!

If we replace r by n in the previous formula, we get the number of permutations of n elements taken n at a time. This we know is $n!$.

$${}_n P_n = n! = \frac{n!}{(n-n)!} = \frac{n!}{0!}$$

For this to be equal to $n!$ the value of $0!$ must be 1.

$0!$ is defined to have a value of 1.

In a region, vehicle license plates consist of 2 different letters followed by 4 different digits. If the letters I, O, Y, and Z are not used, determine how many different license plates are possible by

- a) the fundamental counting principle b) permutations

In many cases involving simple permutations, the fundamental counting principle can be used in place of the permutation formulas.

Complete Assignment Questions #7 - #14

Assignment

1. Without using a calculator, determine the value of

- a) $5!$ b) $\frac{10!}{8!}$ c) $\frac{99!}{100!}$

2. Express as single factorials.

- a) $6 \times 5 \times 4 \times 3 \times 2 \times 1$ b) $9 \times 8 \times 7 \times 6!$ c) $(n+2)(n+1)n(n-1) \dots \times 3 \times 2 \times 1$

3. Express as a quotient of factorials:

- a) $9 \times 8 \times 7 \times 6$ b) $20 \times 19 \times 18$ c) $(n+2)(n+1)n$

4. Use a calculator to determine the exact value of the following:

a) $10!$ b) $\frac{8!}{4!}$ c) $\frac{15!}{10! 5!}$ d) $\binom{25!}{21!} \binom{7!}{11!}$

5. Simplify the following expressions. Leave the answer in product form where appropriate.

a) $\frac{n!}{n}$ b) $\frac{(n-3)!}{(n-2)!}$ c) $\frac{(n+1)!}{(n-1)!}$ d) $\frac{(3n)!}{(3n-2)!}$

6. Solve the equation.

a) $\frac{(n+1)!}{n!} = 6$

b) $(n+1)! = 6(n-1)!$

c) $\frac{(n+2)!}{n!} = 12$

d) $\frac{(n+1)!}{(n-2)!} = 20(n-1)$

7. Determine the number of arrangements that can be made using all of the letters in the word:
- a) DOG b) DUCK c) SANDWICH d) CANMORE
8. Consider the number of five-digit numbers that can be made from the digits 2, 3, 4, 7, and 9 if no digit can be repeated. Express your answer using
- a) factorial notation b) ${}_nP_r$ notation c) the fundamental counting principle
9. a) Use the formula for ${}_nP_r$ to show that ${}_7P_0 = 1$.
- b) Explain why n must be greater than or equal to r in the notation ${}_nP_r$.
10. In each case determine the number of arrangements of the given letters by
- i) using the fundamental counting principle ii) writing in ${}_nP_r$ form and evaluating
- a) two letters from the word **GOLDEN** b) three letters from the word **CHAPTERS**
- c) four letters from the word **WEALTH** d) one letter from the word **VALUE**
11. How many numbers (up to a maximum of four digit numbers) can be made from the digits 2, 3, 4, and 5 if no digit can be repeated?

Multiple Choice

12. In a ten-team basketball league, each team plays every other team twice, once at home and once away. The number of games that are scheduled is

- A. 45
- B. 90
- C. 100
- D. 180

13. The value of ${}_n P_2$ is

- A. $\frac{n}{n-2}$
- B. $\frac{n!}{2!}$
- C. $\frac{n}{2}$
- D. $n(n-1)$

Numerical Response

14. In a competition on the back of a cereal packet, seven desirable qualities for a kitchen (eg. spaciousness, versatility, etc.) must be put in order of importance. The number of different entries that must be completed in order to ensure a winning order is _____.

(Record your answer in the numerical response box from left to right.)

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Answer Key

1. a) 120 b) 90 c) $\frac{1}{100}$ 2. a) 6! b) 9! c) $(n+2)!$
3. a) $\frac{9!}{5!}$ b) $\frac{20!}{17!}$ c) $\frac{(n+2)!}{(n-1)!}$ 4. a) 3 628 800 b) 1680 c) 3003 d) $\frac{115}{3}$
5. a) $(n-1)!$ b) $\frac{1}{n-2}$ c) $n(n+1)$ d) $3n(3n-1)$
6. a) $n=5$ b) $n=2$ c) $n=2$ d) $n=4$
7. a) 6 b) 24 c) 40 320 d) 5040
8. a) 5! b) ${}_5 P_3$ c) $5 \times 4 \times 3 \times 2 \times 1 = 120$
9. a) ${}_7 P_0 = \frac{7!}{(7-0)!} = \frac{7!}{7!} = 1$
- b) You cannot arrange more elements than the number of elements there are to begin with.
10. a) ${}_6 P_2 = 30$ b) ${}_8 P_3 = 336$ c) ${}_6 P_4 = 360$ d) ${}_5 P_1 = 5$

11. 64 12. B 13. D 14.

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